

I'm not robot!

1. In each of the following cases, determine the direction cosines of the normal to the plane and the distance from the origin.

(a)  $x = 2$  (b)  $x + y + z = 1$   
 (c)  $2x + 3y - z = 5$  (d)  $5y + 8 = 0$

Sol. (a) Given: Equation of the plane is  $x = 2$

Let us first reduce it to vector form  $\vec{r} \cdot \vec{n} = d$   
 where  $d > 0$

or  $0x + 0y + 1z = 2$  (Here  $d = 2 > 0$ )

$$\Rightarrow (x\hat{i} + y\hat{j} + z\hat{k}) \cdot (0\hat{i} + 0\hat{j} + \hat{k}) = 2$$

$$(\because a_1a_2 + b_1b_2 + c_1c_2 = (a_1\hat{i} + b_1\hat{j} + c_1\hat{k}) \cdot (a_2\hat{i} + b_2\hat{j} + c_2\hat{k}))$$

$$\Rightarrow \vec{r} \cdot \vec{n} = 2 \text{ where we know that}$$

$$\vec{r} = x\hat{i} + y\hat{j} + z\hat{k} = (\text{Position vector of point } P(x, y, z))$$

$$\text{and here } \vec{n} = 0\hat{i} + 0\hat{j} + \hat{k}$$

$$\text{Now let us reduce } \vec{r} \cdot \vec{n} = d \text{ to } \vec{r} \cdot \hat{n} = p$$

$$\text{Dividing both sides by } |\vec{n}|, \frac{\vec{r} \cdot \vec{n}}{|\vec{n}|} = 2$$

$$\text{i.e., } \vec{r} \cdot \hat{n} = 2 = p \text{ where } \hat{n} = \frac{\vec{n}}{|\vec{n}|} = \frac{0\hat{i} + 0\hat{j} + \hat{k}}{\sqrt{0+0+1}} = 1$$

$$\text{i.e., } \hat{n} = 0\hat{i} + 0\hat{j} + \hat{k} \text{ and } p = 2$$

$\therefore$  By definition, direction cosines of normal to the plane are coefficients of  $\hat{i}, \hat{j}, \hat{k}$  in  $\hat{n}$  i.e., 0, 0, 1 and length of perpendicular from the origin to the plane is  $p = 2$ .

(b) Given: Equation of the plane is  $x + y + z = 1$

$$\Rightarrow 1x + 1y + 1z = 1 \text{ (Here } d = 1 > 0)$$

$$\Rightarrow (x\hat{i} + y\hat{j} + z\hat{k}) \cdot (\hat{i} + \hat{j} + \hat{k}) = 1$$

$$\text{i.e., } \vec{r} \cdot \vec{n} = 1 \text{ where } \vec{n} = \hat{i} + \hat{j} + \hat{k}$$

Dividing both sides by  $|\vec{n}| = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$ , we have

$$\vec{r} \cdot \frac{\vec{n}}{|\vec{n}|} = \frac{1}{|\vec{n}|}$$

[ $\because$  The lost card is a diamond, therefore, there are 12 diamond cards in the remaining pack of 51 cards]

$$\text{and } P(A/E_2) = \frac{{}^{13}C_2}{{}^{51}C_2} = \frac{13 \times 12}{51 \times 50} = \frac{156}{2550}$$

[ $\because$  The lost card is not a diamond, therefore, there are 13 diamond cards in the remaining pack of 51 cards]

We have to find  $P(E_1/A)$  i.e., P(lost card is a diamond card given that the two cards drawn from the remaining pack of 51 cards are diamonds)

We know that

$$P(E_1/A) = \frac{P(E_1)P(A/E_1)}{P(E_1)P(A/E_1) + P(E_2)P(A/E_2)} \text{ (By Baye's Theorem)}$$

$$= \frac{\frac{1}{4} \times \frac{132}{2550}}{\frac{1}{4} \times \frac{132}{2550} + \frac{3}{4} \times \frac{156}{2550}}$$

$$\text{Multiplying every term by } 4 \times 2550, = \frac{132}{132 + 468} = \frac{132}{600} = \frac{11}{50}$$

13. Probability that A speaks truth is  $\frac{4}{5}$ . A coin is tossed. A reports that a head appears. The probability that actually there was head is

(A)  $\frac{4}{5}$  (B)  $\frac{1}{2}$  (C)  $\frac{1}{5}$  (D)  $\frac{2}{5}$

Sol. Let event  $E_1$ : a head appears on a coin.

and  $E_2 = E_1'$ : a head does not appear

then  $E_1, E_2$  are mutually exclusive and exhaustive events

$$P(E_1) = P(E_2) = \frac{1}{2}$$

Let event H: (Person) A reports that a head appears

Given:  $P(H/E_1) = P(\text{Person A reports that a head appears when actually there is head}) = P(\text{A speaks truth}) = \frac{4}{5}$

$$\text{and hence } P(H/E_2) = P(\text{A tells a lie}) = 1 - \frac{4}{5} = \frac{1}{5}$$

we have to find  $P(E_1/H) = P(\text{A head (actually) appears; reported that a head has appeared})$

We know that

$$P(E_1/H) = \frac{P(E_1)P(H/E_1)}{P(E_1)P(H/E_1) + P(E_2)P(H/E_2)} \text{ (By Baye's Theorem)}$$

$$\begin{aligned}
 &= e^{6x} [-3 \cos 3x - 3 - 6 \sin 3x \cdot 3] \\
 &\quad + (-3 \sin 3x + 6 \cos 3x) e^{6x} \cdot 6 \\
 &= e^{6x} (-9 \cos 3x - 18 \sin 3x - 18 \sin 3x + 36 \cos 3x) \\
 &= e^{6x} (27 \cos 3x - 36 \sin 3x) \\
 &= 9e^{6x} (3 \cos 3x - 4 \sin 3x).
 \end{aligned}$$

8.  $\tan^{-1} x$ .Sol. Let  $y = \tan^{-1} x$ 

$$\therefore \frac{dy}{dx} = \frac{1}{1+x^2}$$

Again differentiating w.r.t.  $x$ ,

$$\begin{aligned}
 \frac{d^2y}{dx^2} &= \frac{d}{dx} \left( \frac{1}{1+x^2} \right) = \frac{(1+x^2) \frac{d}{dx}(1) - 1 \frac{d}{dx}(1+x^2)}{(1+x^2)^2} \\
 &= \frac{(1+x^2)(0) - (2x)}{(1+x^2)^2} = \frac{-2x}{(1+x^2)^2}.
 \end{aligned}$$

9.  $\log(\log x)$ .Sol. Let  $y = \log(\log x)$ 

$$\begin{aligned}
 \therefore \frac{dy}{dx} &= \frac{1}{\log x} \frac{d}{dx} \log x \quad \left[ \because \frac{d}{dx} \log f(x) = \frac{1}{f(x)} \frac{d}{dx} f(x) \right] \\
 &= \frac{1}{\log x} \cdot \frac{1}{x} = \frac{1}{x \log x}
 \end{aligned}$$

Again differentiating w.r.t.  $x$ ,

$$\begin{aligned}
 \frac{d^2y}{dx^2} &= \frac{(x \log x) \frac{d}{dx}(1) - 1 \frac{d}{dx}(x \log x)}{(x \log x)^2} \\
 &= \frac{(x \log x) \cdot 0 - \left[ x \frac{d}{dx} \log x + \log x \frac{d}{dx}(x) \right]}{(x \log x)^2} \\
 &= - \frac{\left[ x \cdot \frac{1}{x} + \log x \cdot 1 \right]}{(x \log x)^2} = - \frac{(1 + \log x)}{(x \log x)^2}.
 \end{aligned}$$

10.  $\sin(\log x)$ .Sol. Let  $y = \sin(\log x)$ 

$$\begin{aligned}
 \therefore \frac{dy}{dx} &= \cos(\log x) \frac{d}{dx}(\log x) = \cos(\log x) \cdot \frac{1}{x} \\
 &= \frac{\cos(\log x)}{x}
 \end{aligned}$$

Again differentiating w.r.t.  $x$ ,

4. The lengths of 40 leaves of a plant are measured correct to the nearest millimetre, and the data obtained is represented in the following table:

Length (in mm)	Number of leaves
118-126	3
127-135	5
136-144	9
145-153	12
154-162	5
163-171	4
172-180	2

Find the median length of the leaves.

(Hint: The data needs to be converted to continuous classes for finding the median, since the formula assumes continuous classes. The classes then change to 117.5-126.5, 126.5-135.5, ..., 171.5-180.5.)

Sol. The data is not continuous, so we make the data continuous.

C.I.	C.I.	$f$	$cf$
118-126	117.5-126.5	3	3
127-135	126.5-135.5	5	8
136-144	135.5-144.5	9	17
145-153	144.5-153.5	12	29
154-162	153.5-162.5	5	34
163-171	162.5-171.5	4	38
172-180	171.5-180.5	2	40
		$N = 40$	

← Median class

$$\frac{N}{2} = \frac{40}{2} = 20, \text{ we locate 20 in } cf \text{ column.}$$







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